

Collision dynamics of ^{87}Rb spin-2 Bose-Einstein condensates

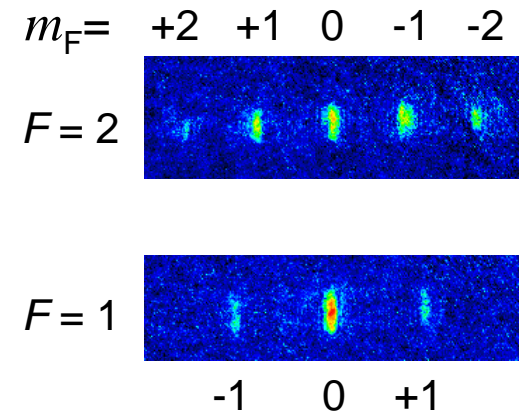
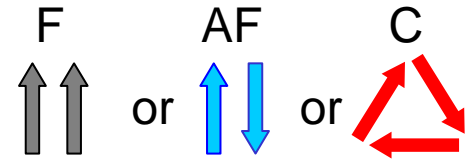
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1-5-1 Mejiro, Toshima-ku, Tokyo 171-8588*



Outline

1. Spin-2 Bose-Einstein condensate (BEC)
 - Motivation: Properties of spin-2 BEC
2. Magnetic phase of spin-2 spinor BEC
 - Spin-population measurement
 - Inelastic collisions of spin-2 BEC
 - Future plan
3. Binary BECs in mixed hyperfine states
 - Two-component BECs in clock states
 -
4. Summary



1. Spin-2 Bose-Einstein condensate

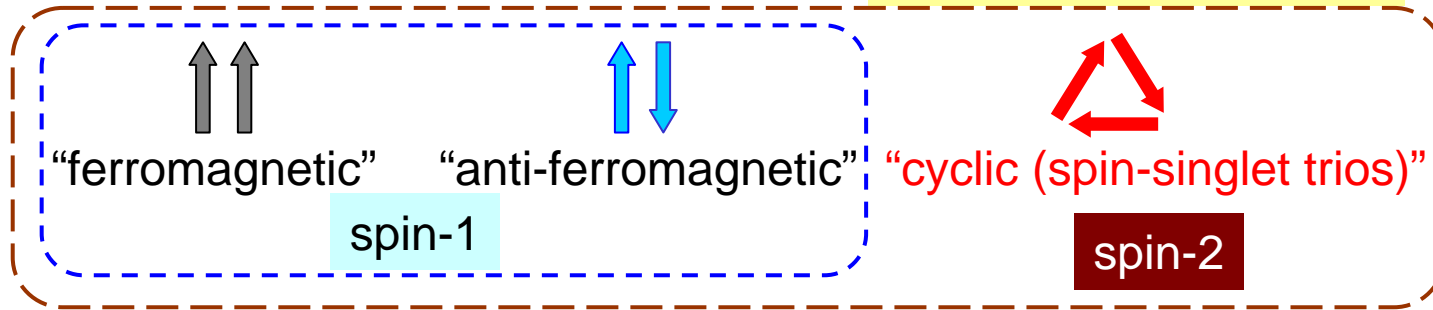
Motivation

Spin-2 Bose-Einstein condensate (BEC)

➡ Novel physics in quantum fluids with spin degree of freedom

Magnetic phases:

New quantum phase!



Ueda & Koashi, *PRA* **65**, 063602 (2002)

Saito & Ueda, *PRA* **72**, 053628 (2005)

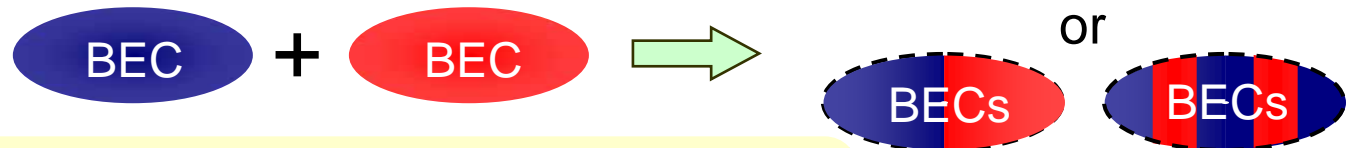
Superfluidity:

- Quantum vortex: multiply charged

$$n = 2 \times |m_F| = 4 \quad \begin{array}{l} n : \text{vorticity,} \\ m_F : \text{magnetic sublevel} \end{array}$$

- Multi-component BEC:

miscible or immiscible (phase-separation)?



Mixed hyperfine states

interplay between different magnetic phases

Motivation

Spin-2 Bose-Einstein condensate (BEC)

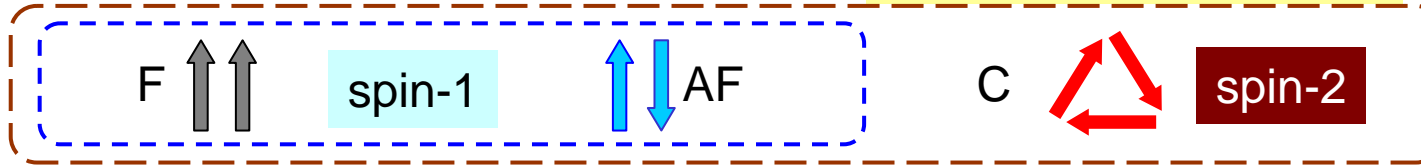
➡ Novel physics in quantum fluids with spin degree of freedom

Magnetic phases:

New quantum phase!

Ueda & Koashi, *PRA* **65**, 063602 (2002)

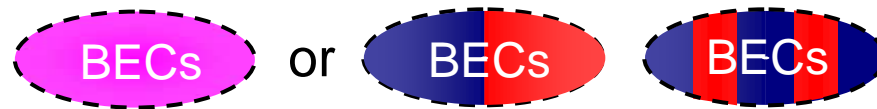
Saito & Ueda, *PRA* **72**, 053628 (2005)



Superfluidity:

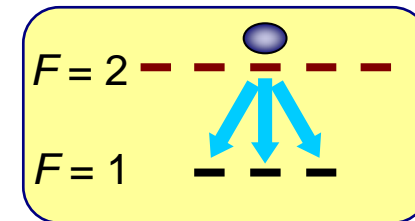
- Quantum vortex: multiply charged
- Multi-component BEC:

miscible or immiscible?



Difficulty in spin-2 BEC

- Unstable BEC for spin-2 systems



trap loss!
Inelastic collisions

Ground state of BEC atoms

- ${}^7\text{Li}$, ${}^{23}\text{Na}$, ${}^{39}\text{K}$, ${}^{87}\text{Rb}$: $F = 1$ ← upper hyperfine levels for $F = 2$
- ${}^{85}\text{Rb}$: $F = 2$, ${}^{133}\text{Cs}$: $F = 3$ ← negative scattering length
- ${}^1\text{H}$: $F = 0$, ${}^4\text{He}^*$, ${}^{174}\text{Yb}$: $J = 0$, ${}^{53}\text{Cr}$: $J = 3$

2. Magnetic phases of spin-2 spinor BEC

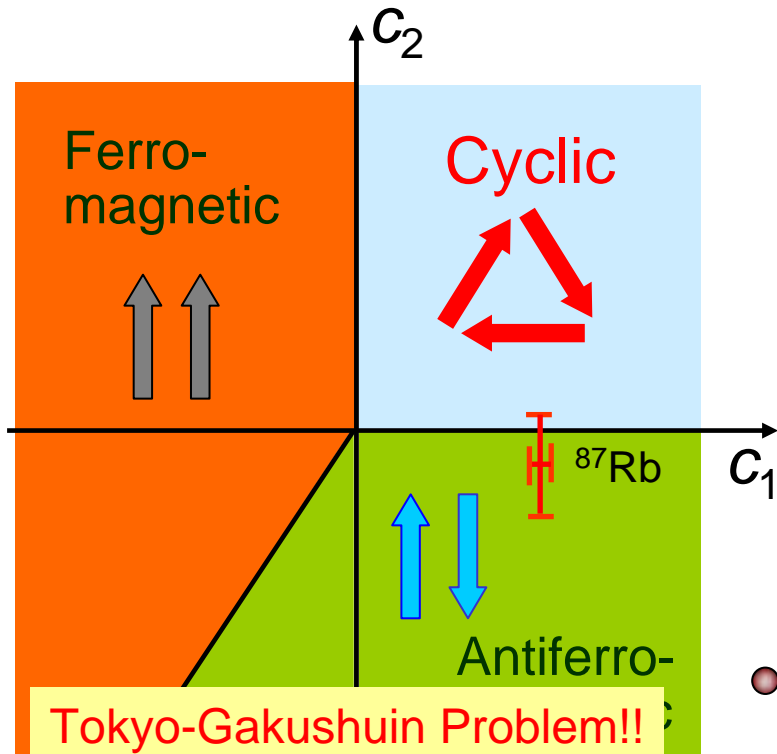
2-1. Spin-population measurement

Magnetic phases in spin-2 system

Phase diagram in spin-2 system

Ueda & Koashi, PRA **65**, 063602 (2002)

Saito & Ueda, PRA **72**, 053628 (2005)



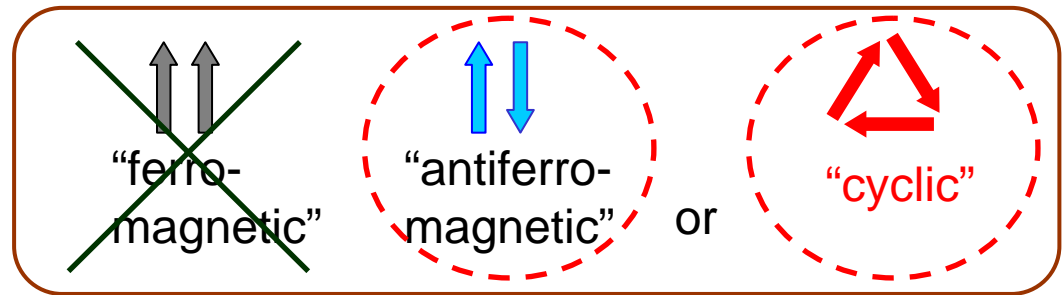
Measured coefficients of spin-dependent interaction

$$c_1 / (4\pi\hbar^2/m) = (+0.99 \pm 0.06) a_B$$

$$c_2 / (4\pi\hbar^2/m) = (-0.53 \pm 0.58) a_B$$

Widera *et al.*, *New Journal of Physics* **8**, 152 (2006)

- Magnetic phases of ^{87}Rb $F = 2$:



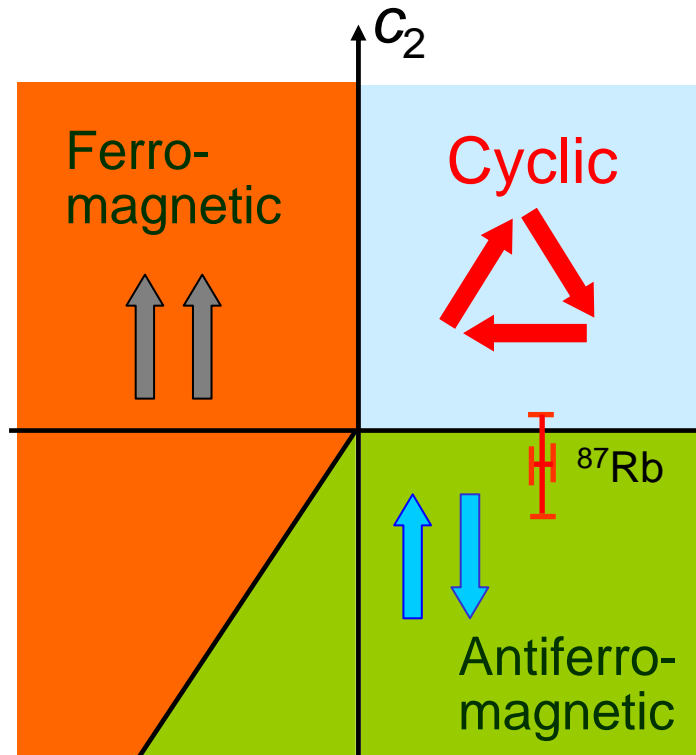
cf. ^{87}Rb $F = 1$  "ferro-magnetic"

$$c_1 = \frac{4\pi\hbar^2}{m} \frac{a_4 - a_2}{7}$$

$$c_2 = \frac{4\pi\hbar^2}{m} \frac{7a_0 - 10a_2 + 3a_4}{7}$$

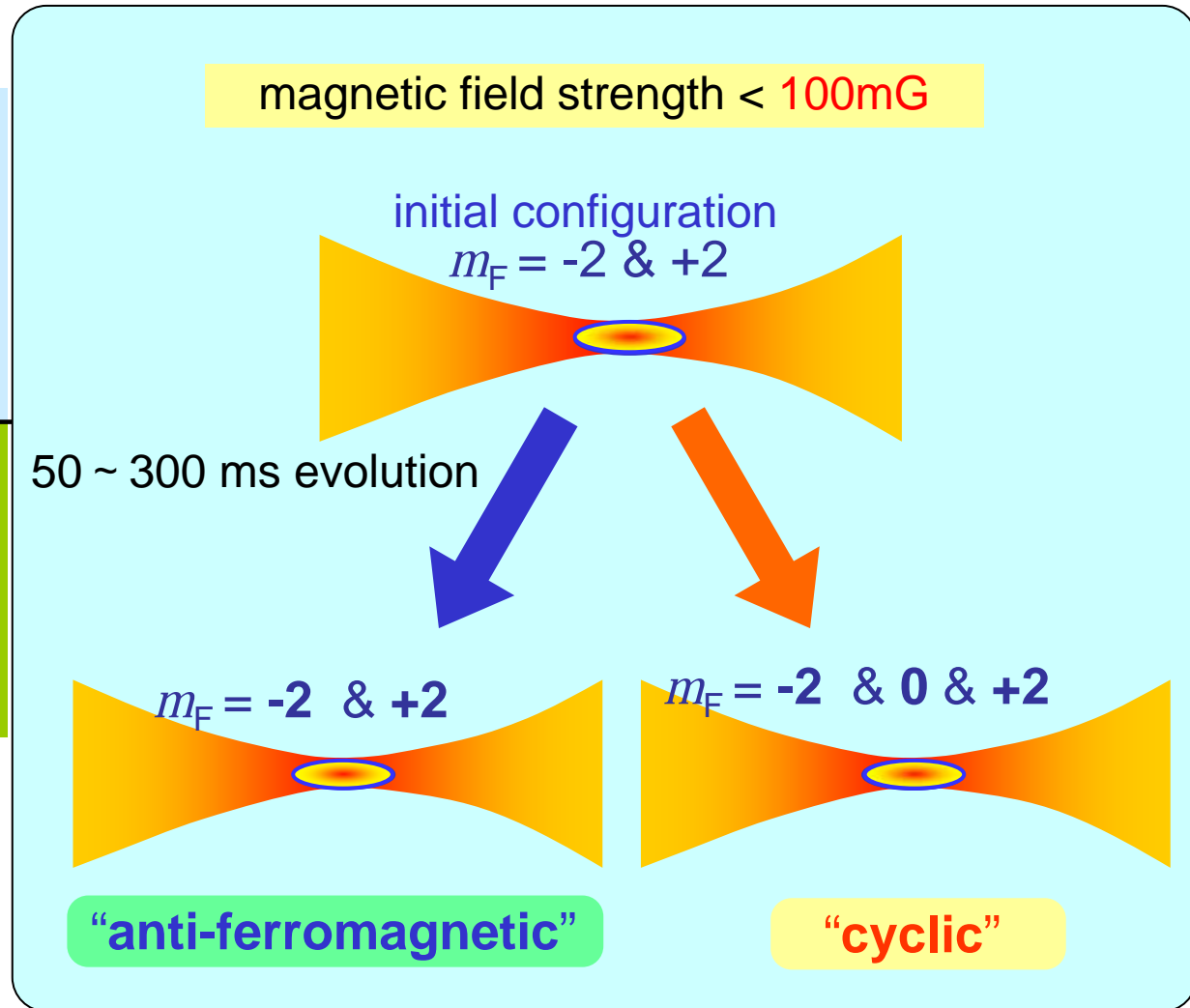
Magnetic phases in ^{87}Rb $F = 2$ BEC

Determination of magnetic phase using spin-population measurement



$$c_1 = \frac{4\pi\hbar^2}{m} \frac{a_4 - a_2}{7}$$

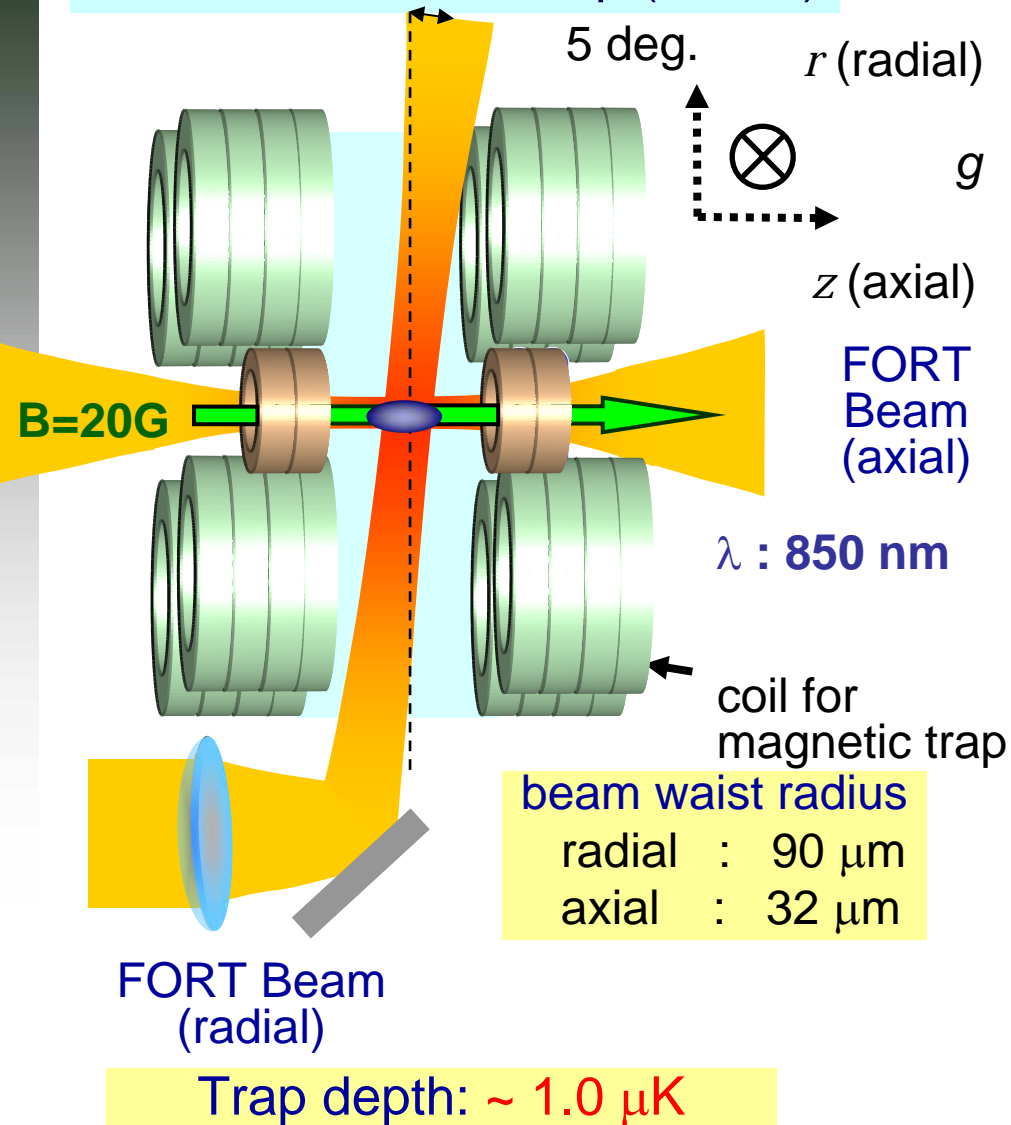
$$c_2 = \frac{4\pi\hbar^2}{m} \frac{7a_0 - 10a_2 + 3a_4}{7}$$



Hiroki Saito & Masahito Ueda
PRA 72, 053628 (2005)

Optical trap (Far-Off Resonant Trap)

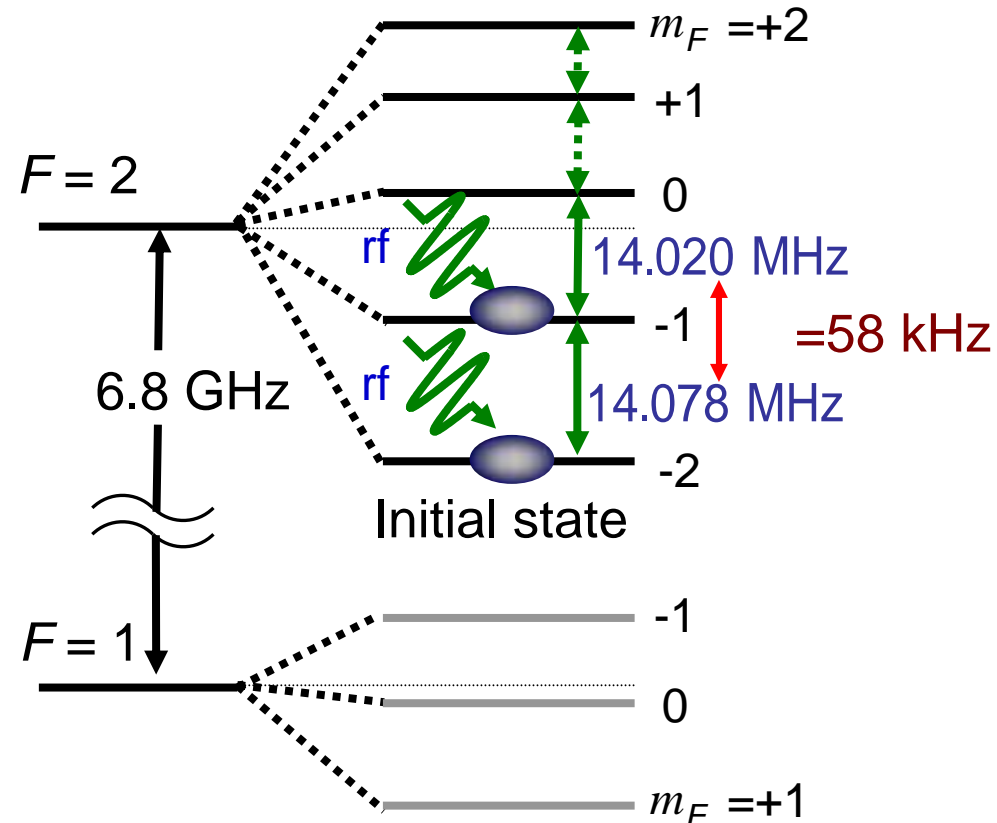
Far-Off Resonant Trap (FORT)



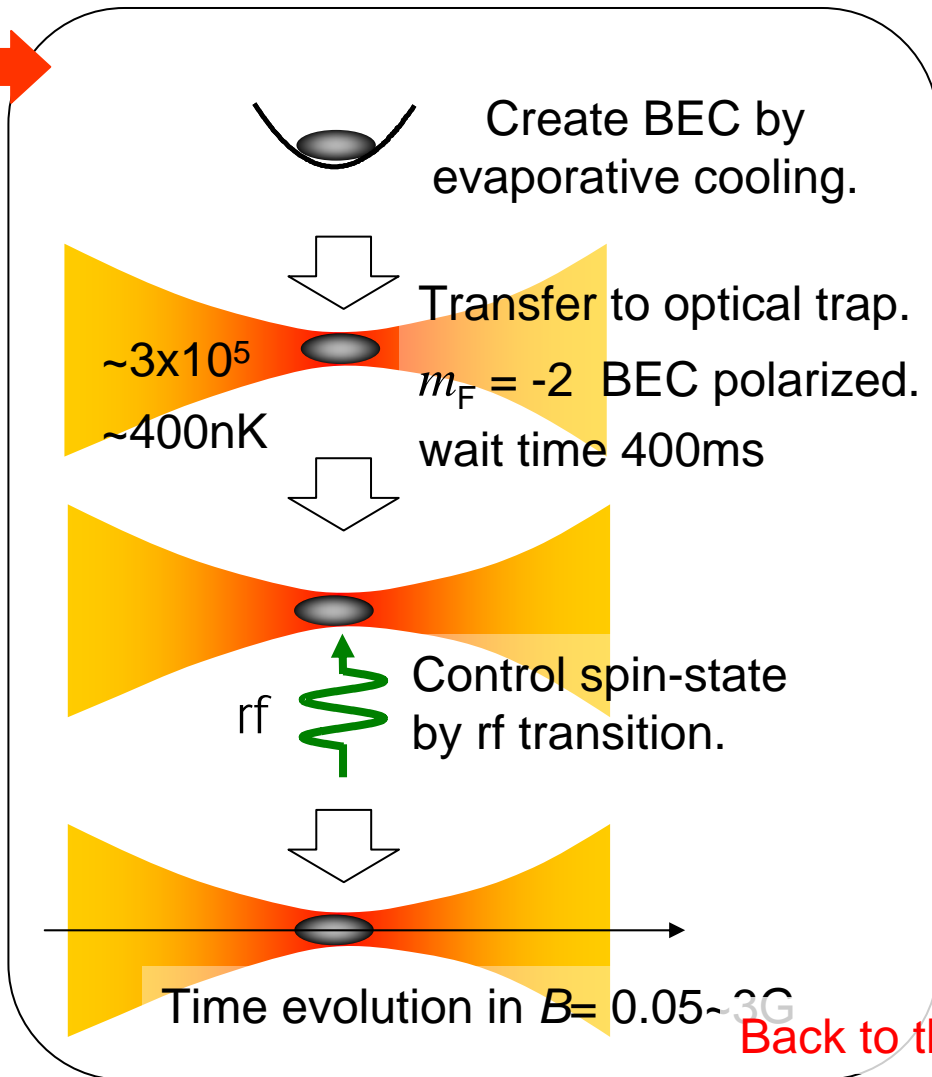
Energy level diagram of ^{87}Rb (ground hyperfine states)

Zeeman splitting at $B = 20\text{ G}$

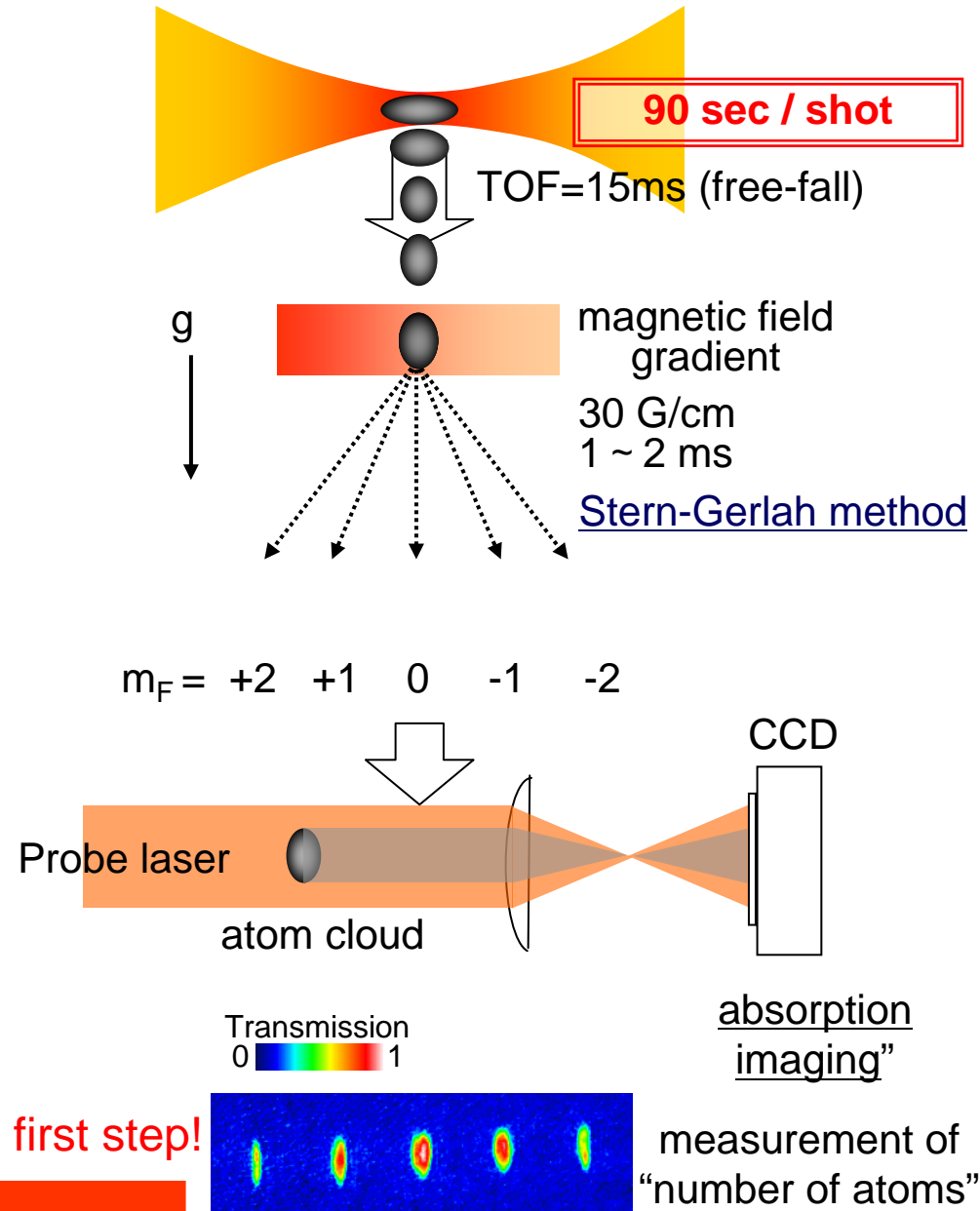
It is possible to selectively prepare any spin-states.



Experimental procedure

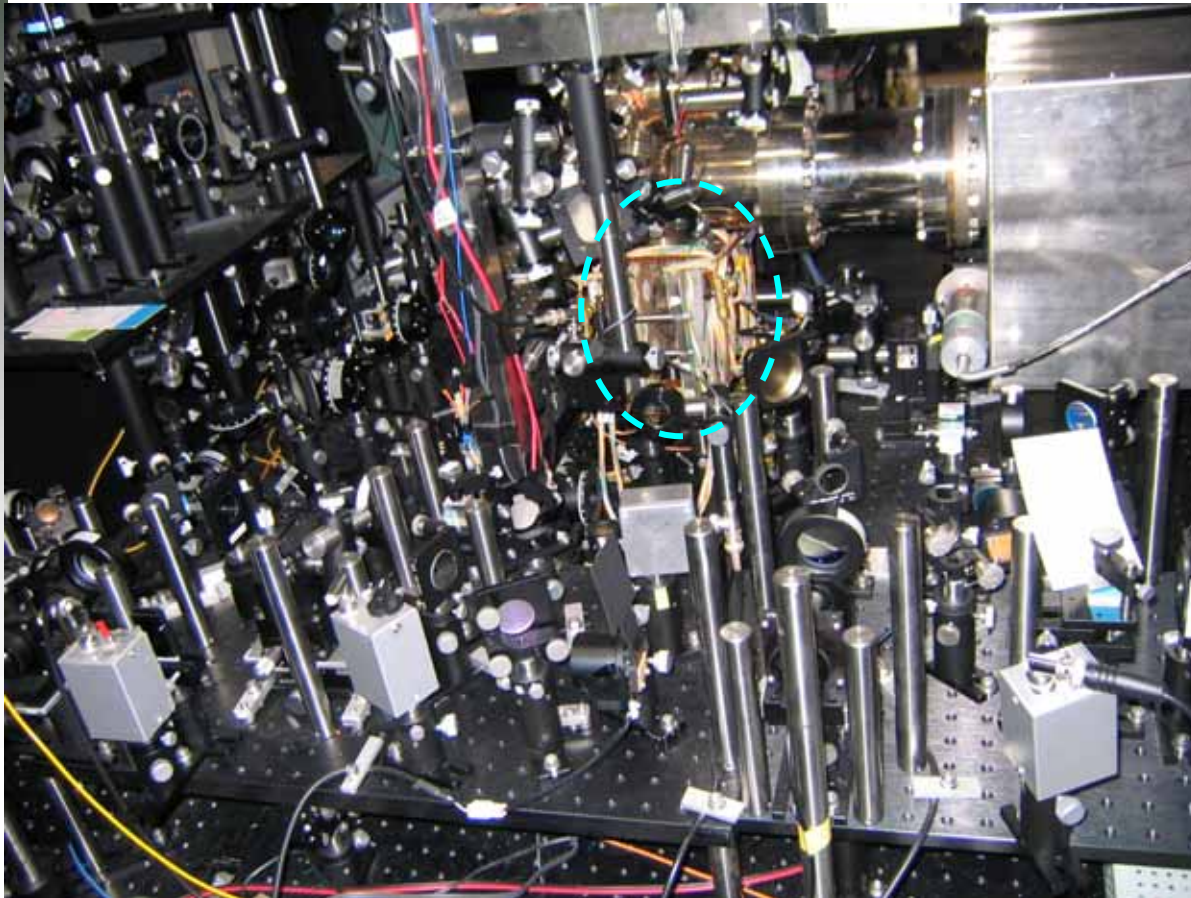


Back to the first step!

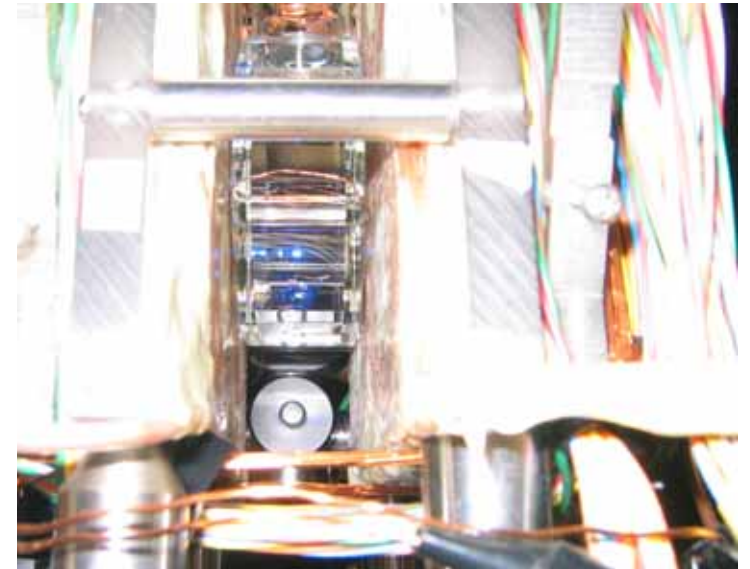


Experimental setup

BEC setup



Main chamber



Evolution of $m_F = -2$ & $m_F = +2$ BEC mixture

magnetic field : 45mG

initial spin-state:

$$|F = 2, m_F = +2\rangle + |F = 2, m_F = -2\rangle$$

Trap time
(ms)

$m_F = +2$

$m_F = -2$

0



50



100



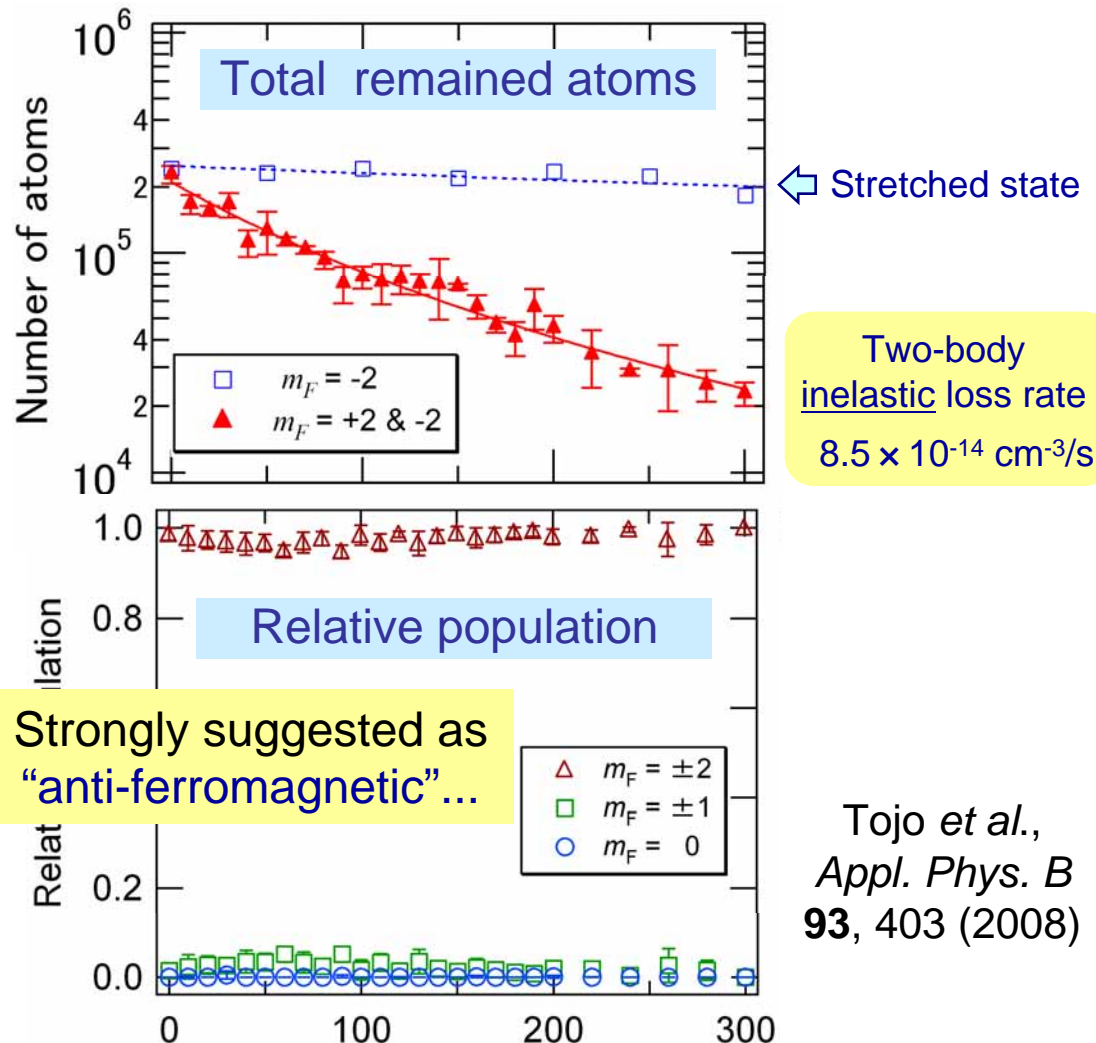
200



300



No other components grew ...



Tojo *et al.*,
Appl. Phys. B
93, 403 (2008)

Inelastic collision rates should be considered!!

e.g. if rate of $|2,0\rangle + |2,-2\rangle \gg |2,+2\rangle + |2,-2\rangle$,
 $|2,0\rangle$ state cannot be observed.

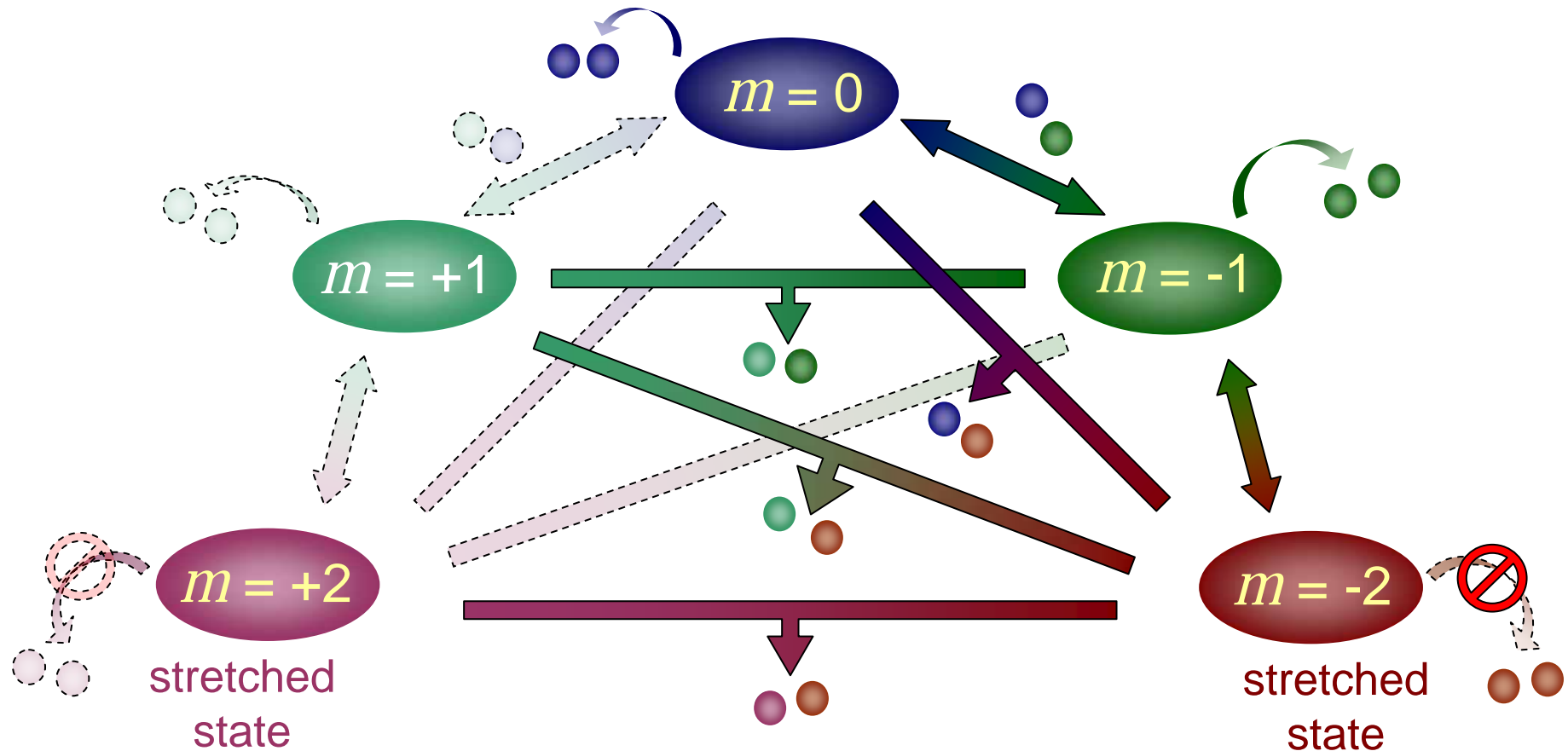
2. Magnetic phases of spin-2 spinor BEC

2-2. Inelastic collisions in spin-2 BEC

Inelastic collision of spin-2 system

- Inelastic collision of spin-2 atoms

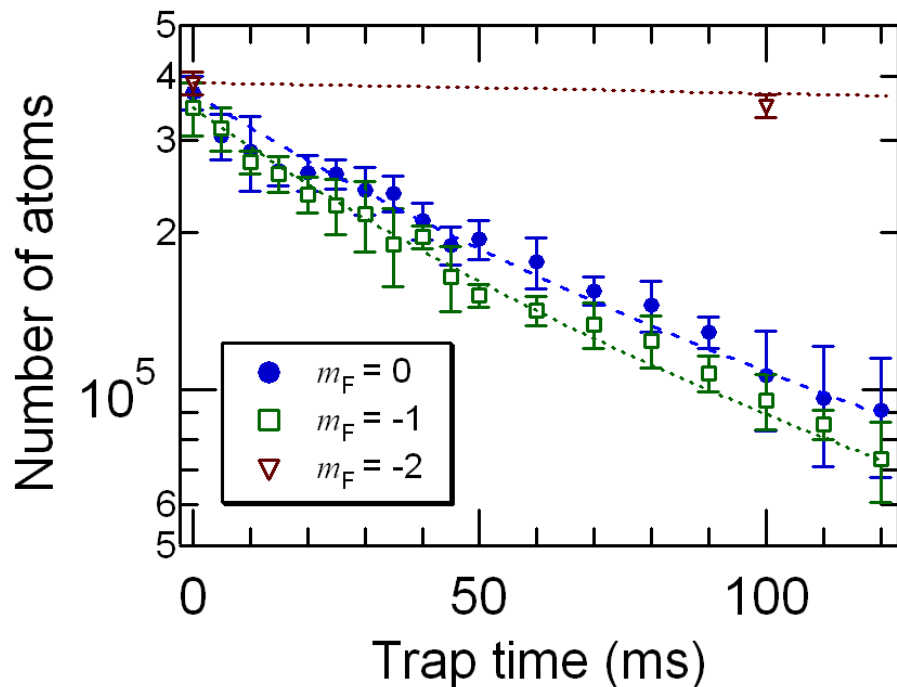
Total spin of collision channel; $\mathcal{F} = 0, 2, 4$



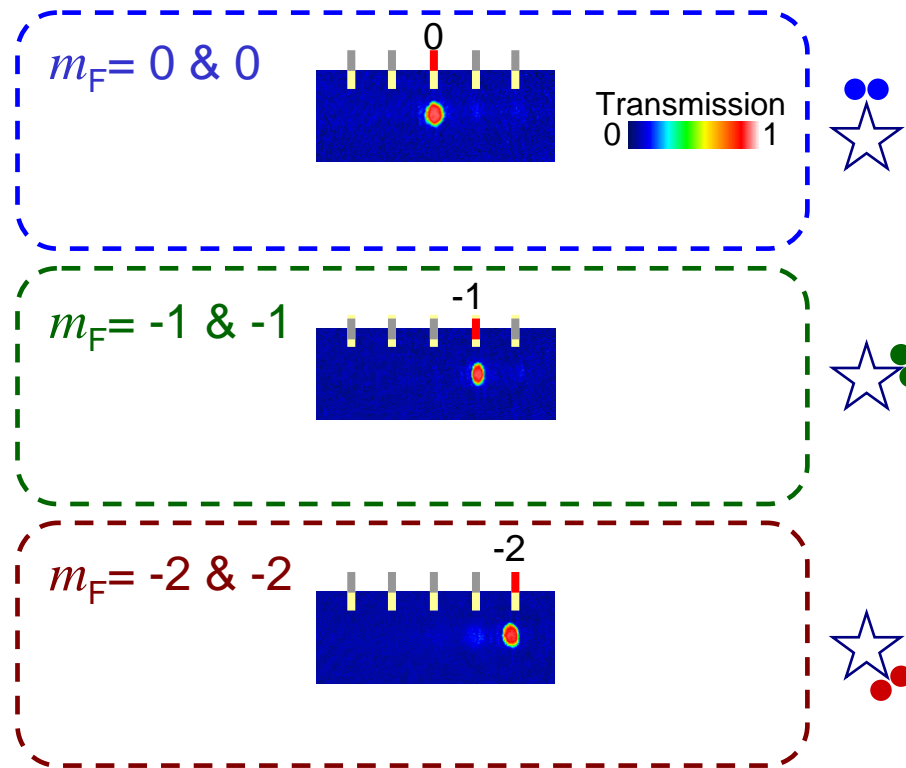
Time-evolution of identical spin state ($m_F = 0, m_F = -1$)

Single component BEC

magnetic field : 3.0 G



- $K_{2(-2,-2)}$ is very small!!
 → Negligible inelastic collision for $|2, -2\rangle + |2, -2\rangle$ (stretched state).
- Difference between $K_{2(0,0)}$ and $K_{2(-1,-1)}$.



Inelastic collision parameters: b_4, b_2, b_0

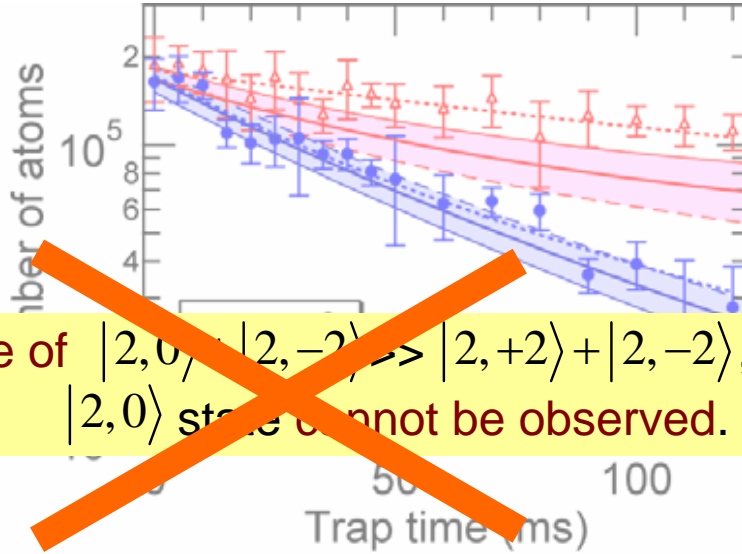
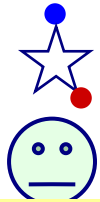
$$b_0 = \quad \times 10^{-14} \text{ cm}^{-3}/\text{s}$$

$$b_2 = \quad \times 10^{-14} \text{ cm}^{-3}/\text{s}$$

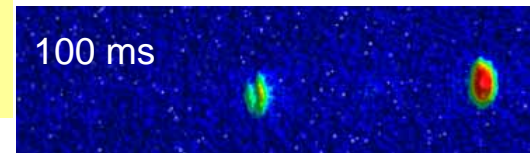
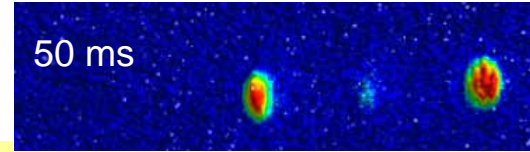
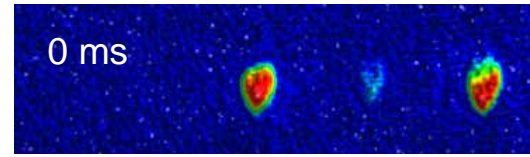
$$b_4 = \quad \times 10^{-14} \text{ cm}^{-3}/\text{s}$$

Atom number evolution in $|2,0\rangle + |2,-2\rangle$ and $|2,0\rangle + |2,-1\rangle$

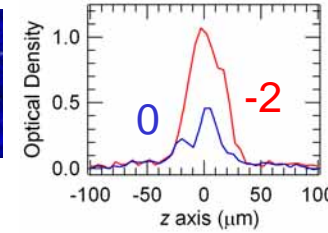
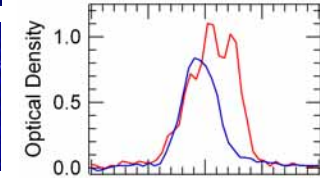
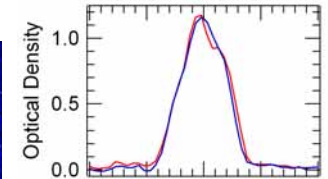
$m_F = 0$ and -2 magnetic field : 3.0 G



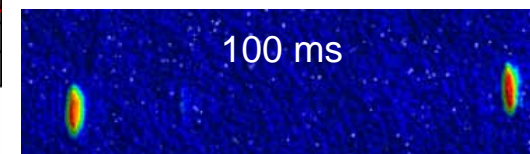
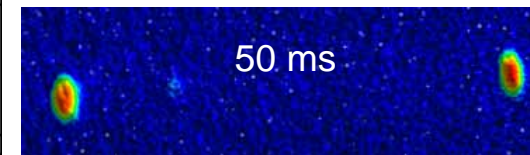
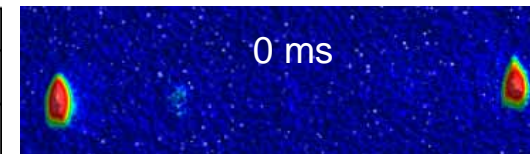
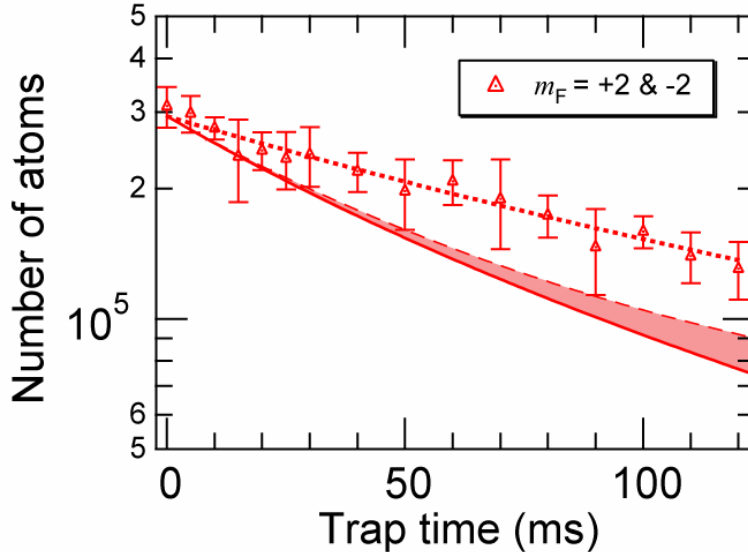
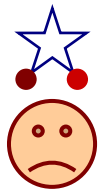
e.g. if rate of $|2,0\rangle + |2,-2\rangle \gg |2,+2\rangle + |2,-2\rangle$, $|2,0\rangle$ state cannot be observed.



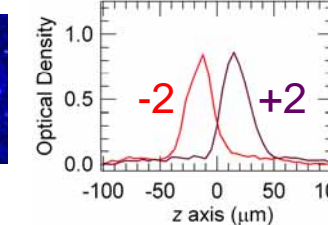
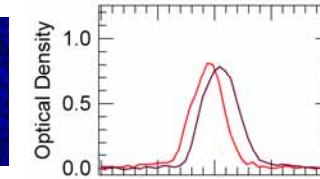
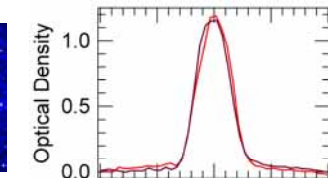
miscible



$m_F = +2$ and -2

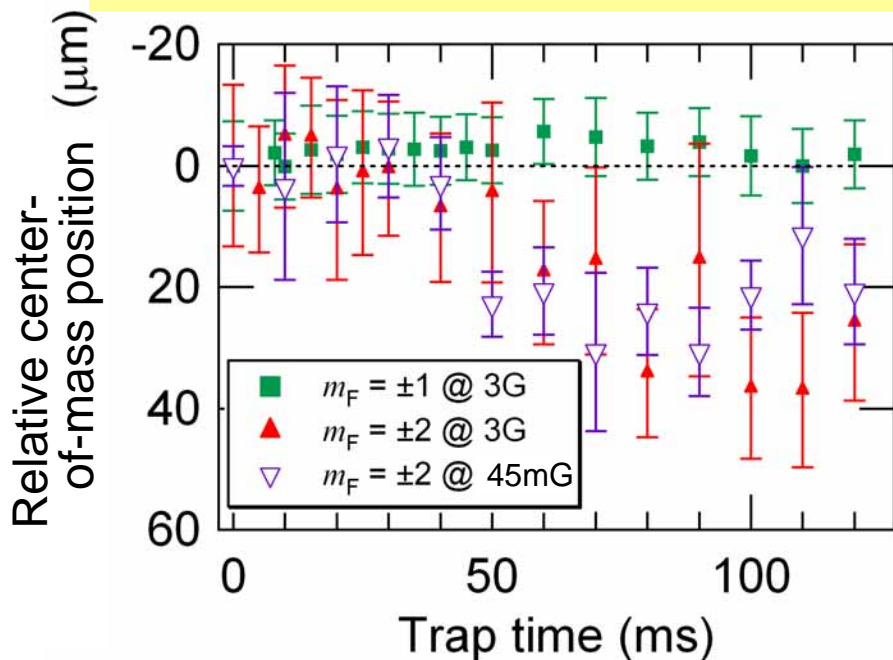


miscible

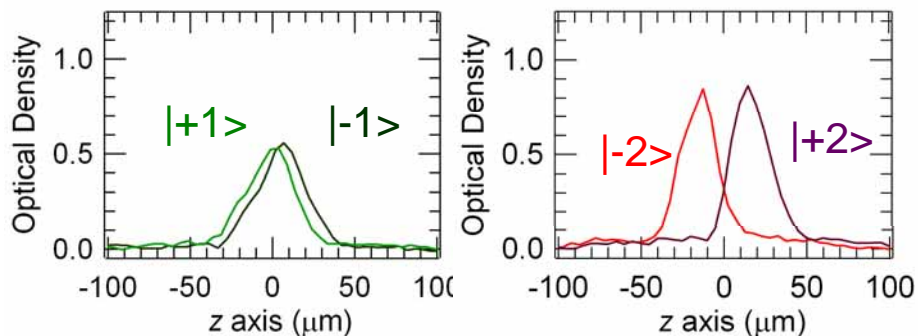


Relative displacement between different spin states

Relative center of mass position



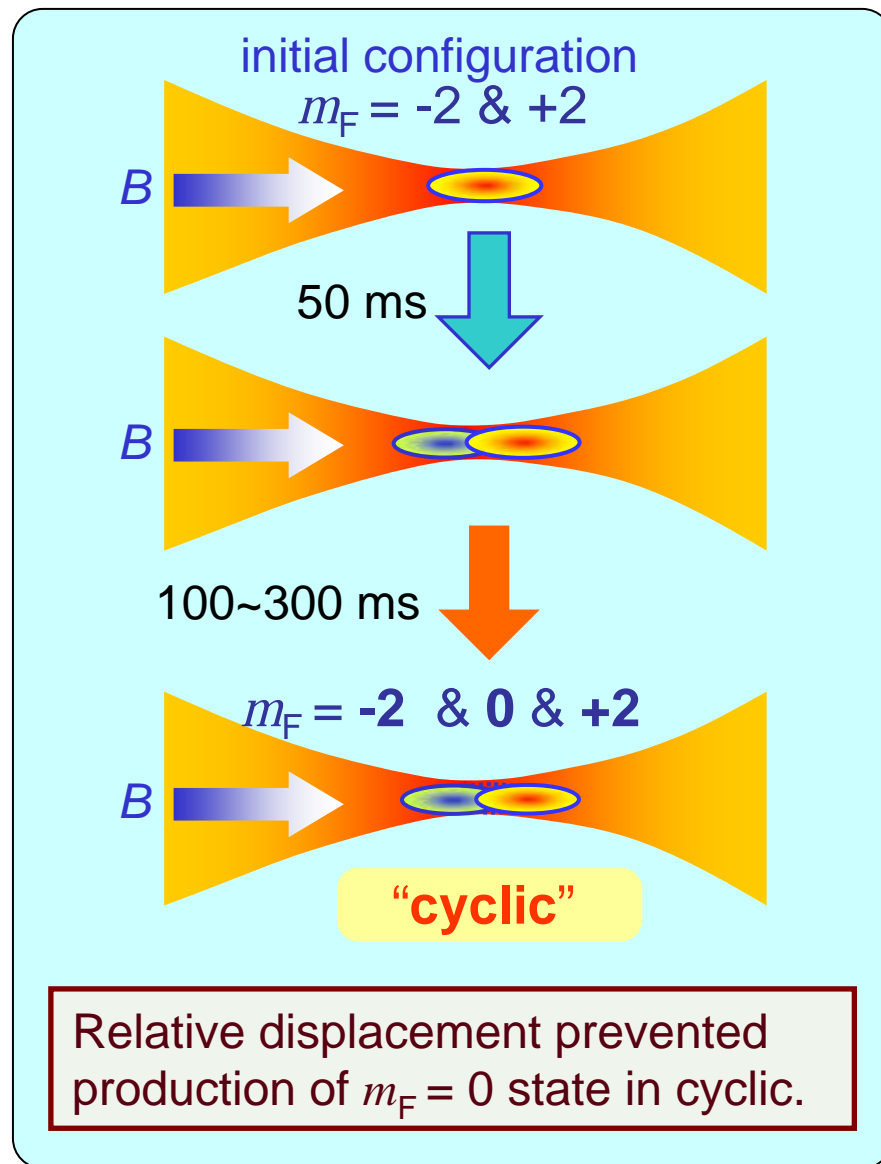
Averaged optical density in z axis at 100ms



overlapped

relative displacement

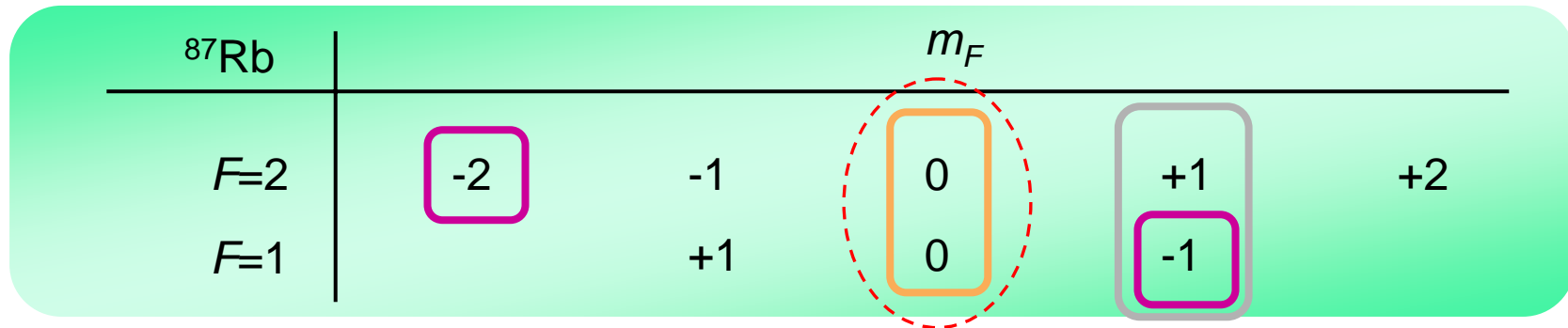
Spin population measurement



3. Binary BECs in mixed hyperfine states

3-1. Two component BECs in clock states

Binary BECs in mixed hyperfine states



Phase separation of 2-component BECs

^{87}Rb $|1,+1\rangle$ & $|2,-1\rangle$

D. S. Hall *et al.*, Phys. Rev. Lett. **81**, 1539 (1998)
K. M. Mertes *et al.*, Phys. Rev. Lett. **99**, 190402 (2007)

^{23}Na $|1,+1\rangle$ & $|1,0\rangle$

H.-J. Miesner *et al.*, Phys. Rev. Lett. **82**, 2228 (1999)
K. Kasamatsu and M. Tsubota., Phys. Rev. Lett. **93**, 100402 (2004)

$|2,-2\rangle$ & $|1,-1\rangle$: oppositely sensitive to magnetic field

$|2,+1\rangle$ & $|1,-1\rangle$: same sensitive to magnetic field

$|2,0\rangle$ & $|1,0\rangle$: insensitive to magnetic field!!

$|2,0\rangle$ + $|1,0\rangle$



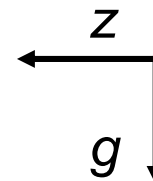
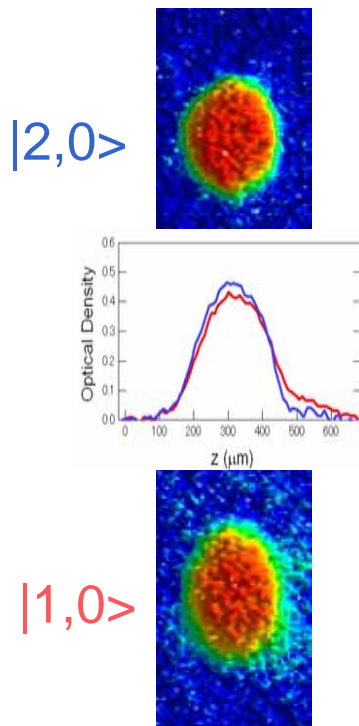
???

We observed time-evolution of $|1,0\rangle + |2,0\rangle$ in optical trap to prevent from effects of magnetic field.

Observation of phase-separation: equal population

$$|1,0\rangle : |2,0\rangle \sim 0.5 : 0.5$$

Time evolution (ms) 0 50 100 150 200

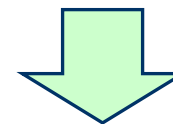


Phase-separation condition

$$\sqrt{a_{11}a_{22}} < a_{12}$$

$$a_{11} = 100.86a_B \quad a_{12} = ??$$
$$a_{22} = 94.57a_B$$

Widera *et al.*,
New J. Phys. **8**, 152 (2006)



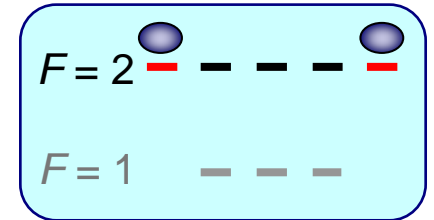
Symmetrically separated each other

$$a_{12} > 97.66a_B ?$$

Summary

- Magnetic phase of ^{87}Rb spin-2 BEC

- For $m_F = \pm 2$ initial state, atoms remain in $m_F = \pm 2$
“Anti-ferromagnetic behavior”



- Inelastic collision rates of all possible channels are well described by two parameters: basis knowledge for future study.

$$b_0 = \quad , \quad b_2 = \quad , \quad b_4 =$$

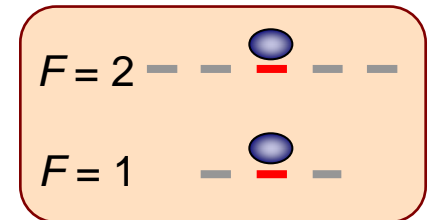
Results supported “anti-ferromagnetic” phase...

However, effects of relative displacement or phase-separation??

➔ Future plan

- **Binary BECs** in mixed hyperfine states

- Multiple domains are observed in **clock states.**





Thank you !!