

# Global Phase Diagram of the 1D Triangular-Lattice Hubbard Model

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Motivated by the recent discovery of spin-triplet superconductivity in a variety of materials such as organic conductors (TMTSF)<sub>2</sub>X and some transition-metal oxides, we study the one-dimensional (1D) Hubbard model with nearest-neighbor  $t_1$  and next-nearest-neighbor  $t_2$  hopping integrals, i.e., 1D triangular-lattice Hubbard model, over a wide parameter and doping regions. We use the density-matrix renormalization group (DMRG) method as well as the Hartree-Fock approximation to calculate the Tomonaga-Luttinger-liquid parameter  $K_\rho$  and the spin gap of the system. Based on the calculated results, we determine the ground-state phase diagram in the strong-coupling regime as shown in Fig. 1. We find that, in contrast to the weak-coupling phase diagram which predicts a spin-gapped liquid phase for a Fermi surface with four points, the spin gap vanishes in a substantial region of the strong-coupling phase diagram. We argue that this result occurs because the ferromagnetic spin fluctuation is induced by the Nagaoka mechanism near half filling and by the three-site ring-exchange interaction for  $t_2 > t_1$  away from half filling. We also find that the spin-singlet superconducting correlation is enhanced near the critical boundary at which the Fermi surface splits from two into four points. Details are given in Refs. [1]-[3].

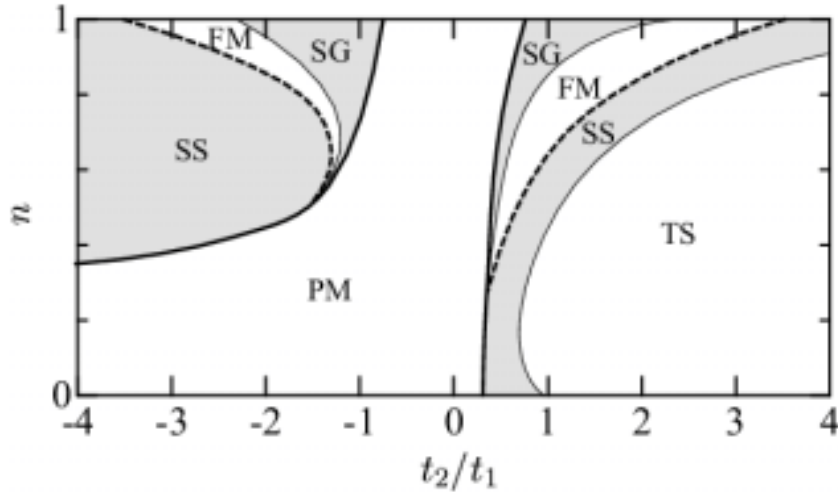


Fig. 5: Calculated phase diagram of the 1D  $t_1 - t_2 - U$  Hubbard model at  $U/t_1 = 10$ . SG: aspin-gapped liquid with incommensurate spiral correlations, FM: a paramagnetic metal with strongferromagnetic fluctuations, SS: spin-singlet superconductivity, TS: spin-triplet superconductivity.

[1] Y. Ohta, S.Nishimoto, T. Shirakawa, and Y. Yamaguchi, Phys. Rev. B **72**, 012503 (2005).

[2] S. Nishimoto, T. Shirakawa, and Y. Ohta, Phys. Rev. B, in press (2007).

[3] S. Nishimoto, K. Sano, and Y. Ohta, in preparation.