

科研費特定領域

「スーパークリーン物質で実現する新しい量子相の物理
キックオフ研究会 2005.12.15-16

量子臨界点近傍に現われる 新奇量子現象の解明

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量子臨界点近傍の物理

新しい量子臨界現象

モット転移 ^3He 単原子層、有機伝導体、遷移金属化合物

電荷秩序転移 有機伝導体、遷移金属酸化物

価数転移 希土類化合物

giant density fluctuation

新奇量子相

ギャップレス量子スピン液体

^3He 単原子層、有機伝導体、遷移金属化合物

Novel Quantum Phase and Criticality

Takahiro Mizusaki

Shinji Watanabe

Kota Hanasaki

Takahiro Misawa

Yohei Yamaji

Masatoshi Imada

Quantum Spin Liquid

Compounds with Geometrical frustration

Suppression of magnetic order,
Large residual entropy

Spin liquid

$$S > 1/2$$

$$S = 1/2$$

Triangular



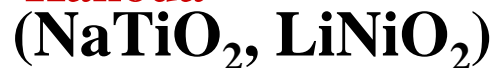
Nambu, Nakatsuji, Maeno



Tamura, Kato



Kanoda



Melzi et al.

^3He on graphite

Greywall, Elser, Fukuyama

Volborthite

Hiroi

$J_1\text{-}J_2$

Kagomè



Obradors et al.

Broholm et al.

Spinel



Greedan et al.

Taguchi, Tokura et al.

Sato et al.



Fukazawa, Maeno



Wiebe et al. *M. IMADA*

Pyrochlore

fcc

Gapless spin liquid

triangular lattice

S=1/2

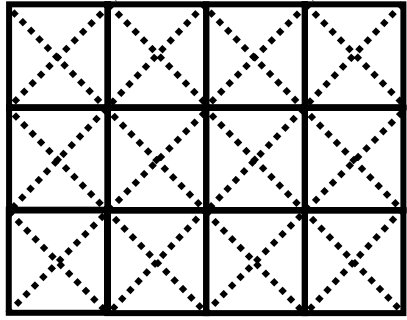
κ -(ET)₂Cu₂(CN)₃ T_1, χ

³He monolayer χ, C

S=1

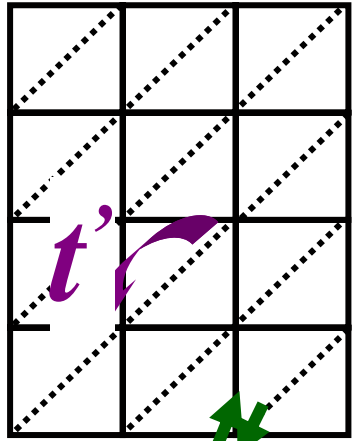
NiGa₂S₄ $\chi, C, \text{neutron}$

Phase Diagram of Frustrated Hubbard Model at $1/2$ Filling



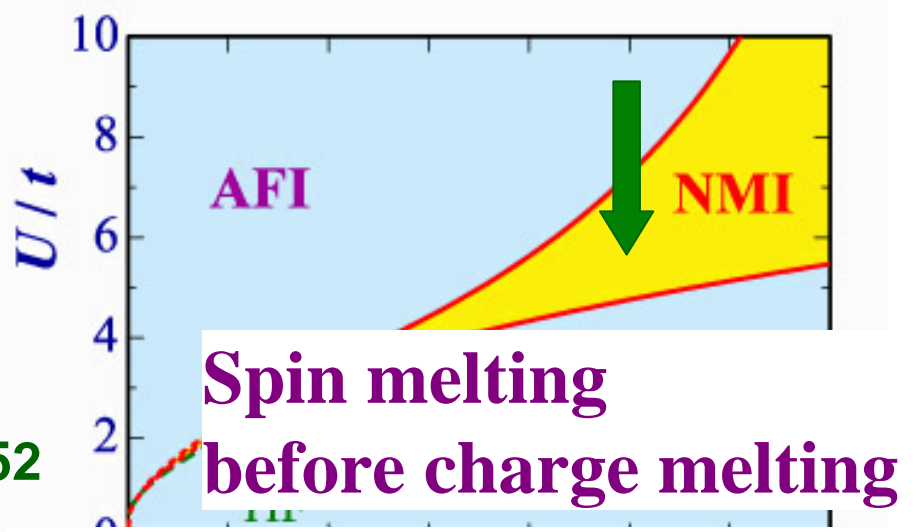
Frustrated square lattice
 Kashima et al.
 JPSJ 70 (2001) 3052

フラストレートした正方格子

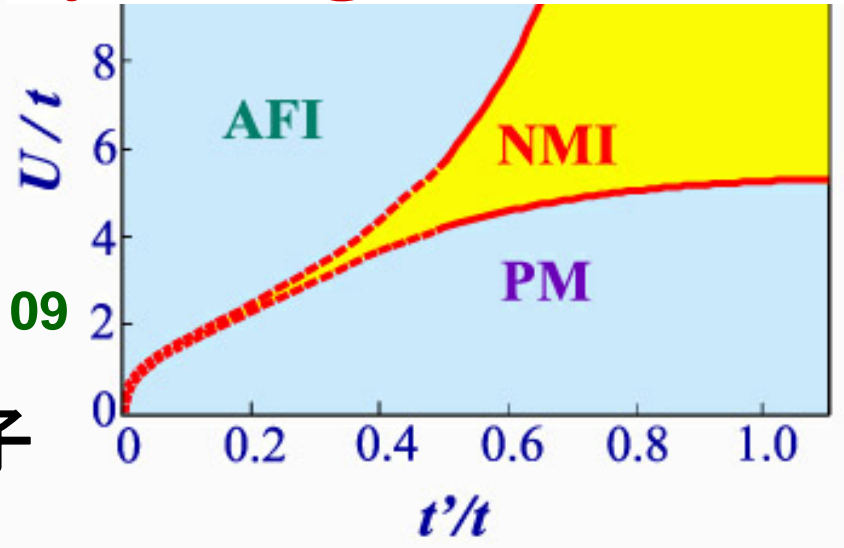


Anisotropic triangular lattice
 Morita et al.
 JPSJ 71(2002) 2109

非等方三角格子



Quantum melting by charge fluctuations



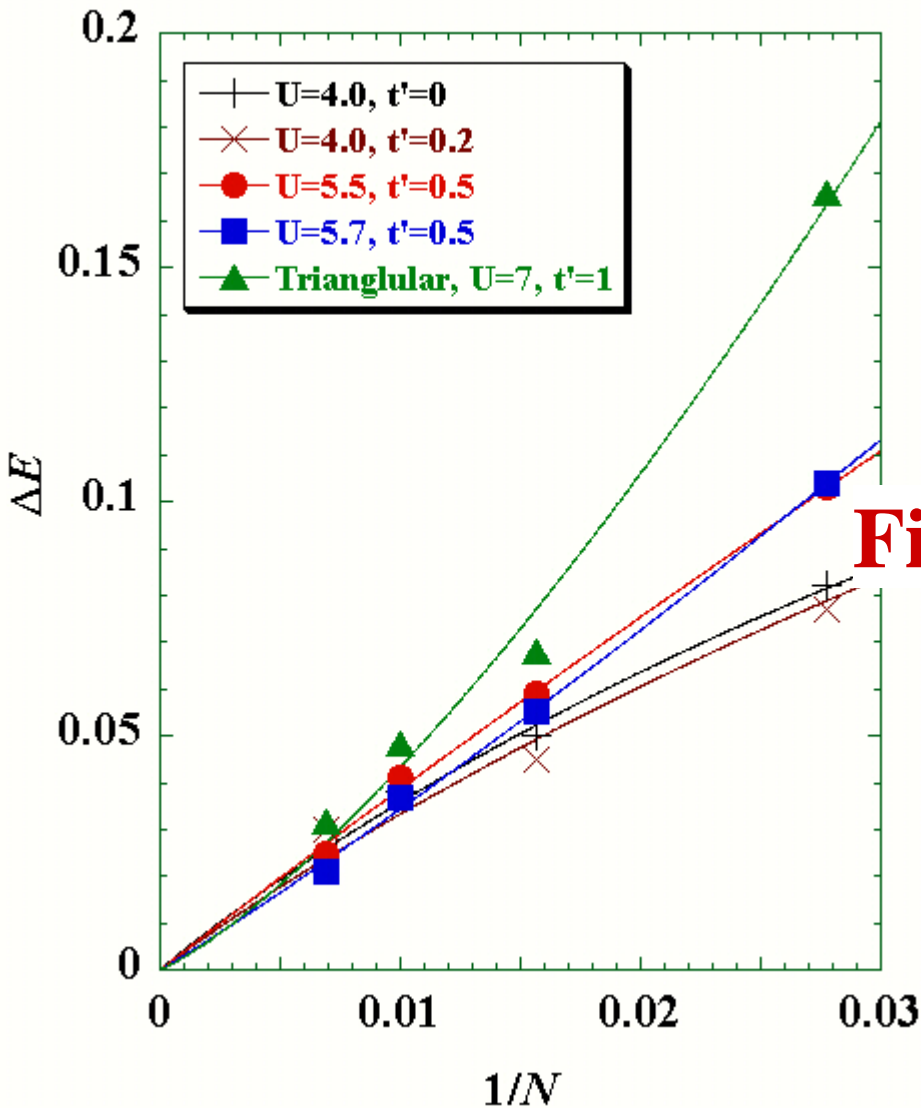
Nonmagnetic Mott insulator phase

Spin-gapless phase

ギャップレス相

gapless spin excitations

Size Scaling of Gap



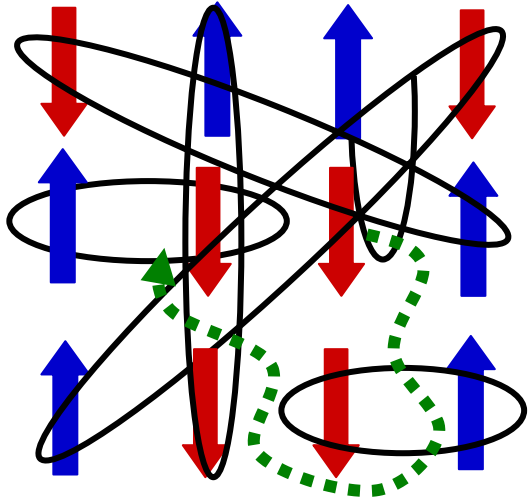
$$\Delta E \sim 1/N$$

Triplet excitation gap collapses
with increasing system size

Long-ranged singlet bonds

Finite uniform susceptibility
有限な一様帯磁率

A possible interpretation of spin liquid



Long-ranged singlet bonds RVB

Gapless spin excitation

Finite, nonzero susceptibility

**Unbound spinon scattered
by sea of dynamical RVB singlets**

Incoherent (localized) spinons?

No spinon Fermi surface?

No fractionalization?

triangular lattice + tiny randomness \Rightarrow spin glass

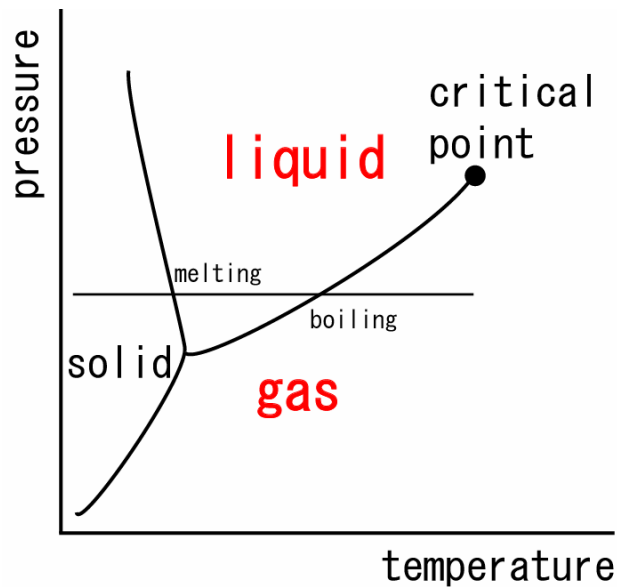
order by disorder

coupling to lattice

MI(1986)
M. IMADA

Novel Quantum Criticality

密度ゆらぎの発散を伴う量子臨界

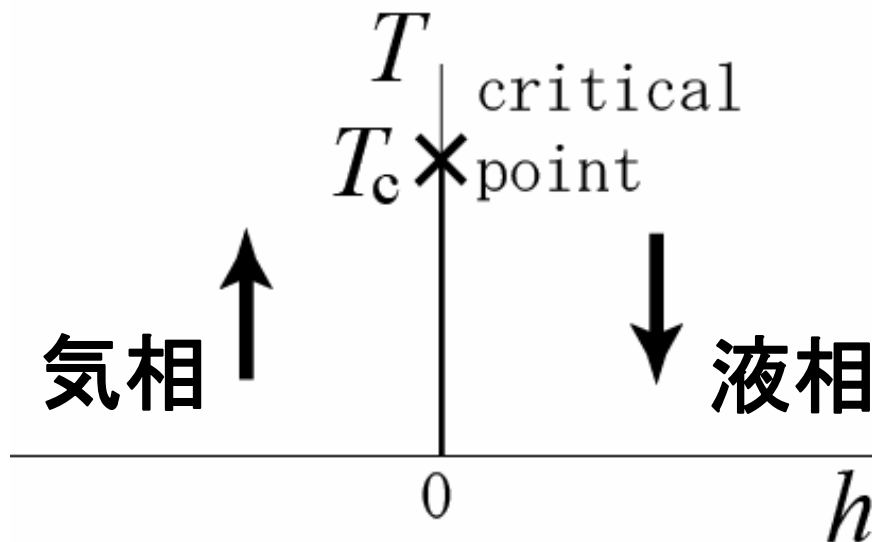


$\chi = dn/d\mu$:
compressibility
の臨界点での発散

気相液相転移の臨界温度が
量子縮退温度以下になるとき？

★ Ising 型相転移として
表わされなくなる場合
non-GLW型

★ 密度ゆらぎ発散と
量子縮退(フェルミ面
効果)の相乗



Valence Criticality

Valence instabilities of Ce systems

Watanabe Poster07
Ce compounds:

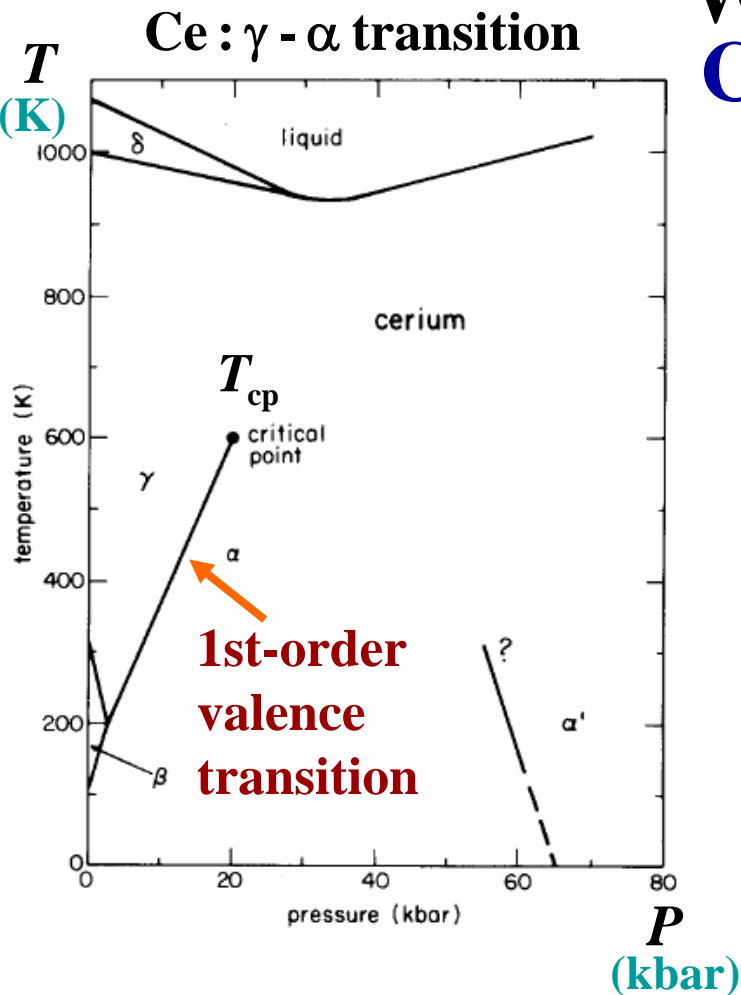
T_{cp} is suppressed ($\ll E_F$)



Superconductivity

CeCu₂Ge₂
CeCu₂Si₂
CeCu₂(Si_{1-x}Ge_x)₂
CeCoIn₅
CeIrIn₅

**Diverging valence fluctuation
+ Fermi degeneracy**



“Handbook on the Physics and Chemistry of Rare Earths”, North-Holland (1978) p340

K. Miyake, et al: PhysicaB 259-261 (1999)676

M. IMADA

Quantum Mott Criticality

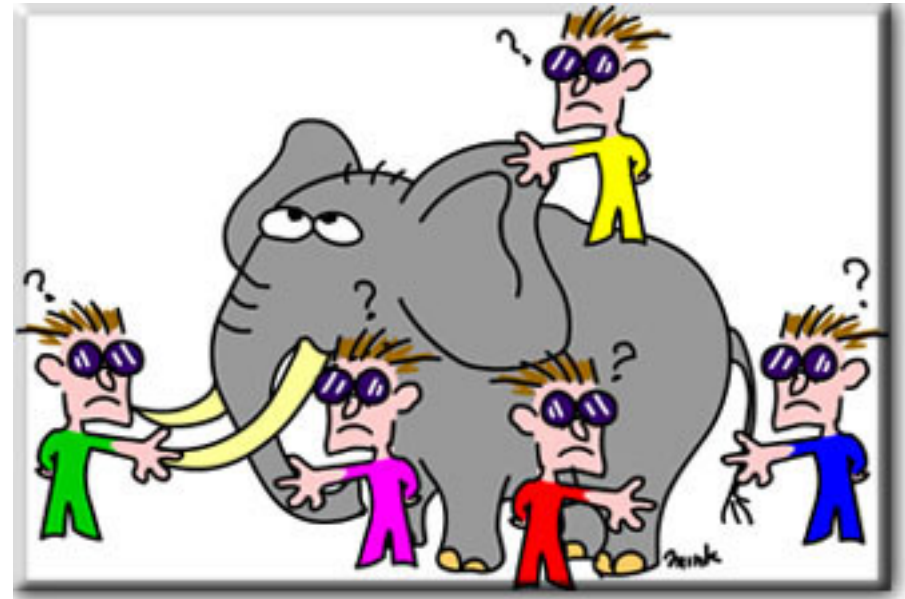
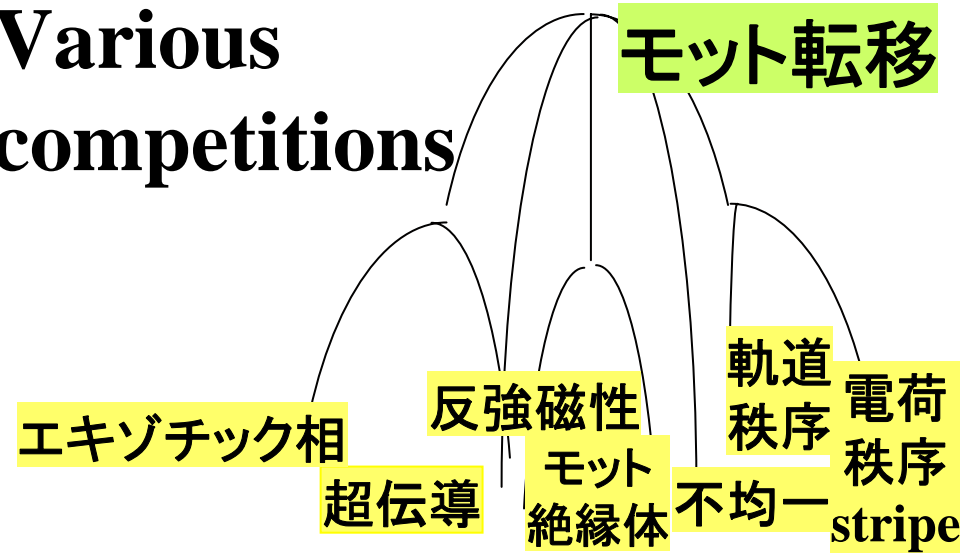
密度ゆらぎの増大+フェルミ面効果 ————→ **Competing Orders**

Breakdown of simple quantum criticality

モット臨界性;
新たな階層構造の原因
母転移→multi-furcation

では大域構造を決める
母転移(モット転移)の
正体は何なのか?

Various
competitions



phase separation

Emery-Kivelson

Physica C 209 (1993) 597

critical divergence of compressibility

Furukawa and MI

JPSJ 61 (1992) 3331

³He monolayer

Saunders et al., Fukuyama

Cuprates

stripe, charge order

Tranquada et al.

Nature 375 (1995) 561

patch structure in STM

Davis et al. (2000)

モット転移は電子の
電荷(密度)自由度の転移
orbital fluctuations

divergence of
single length scale ξ ;
mean distance of carriers
scaling theory & hyperscaling

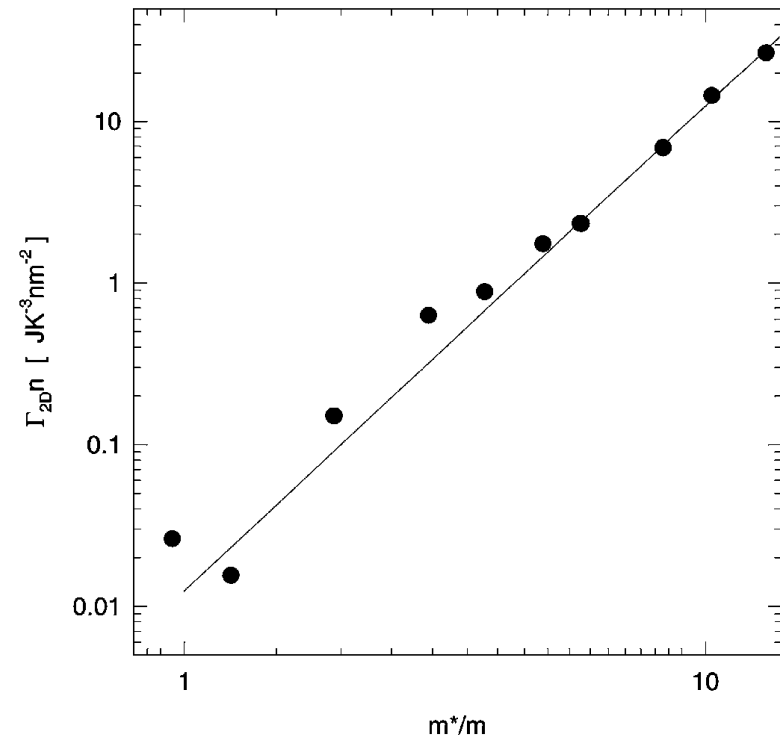
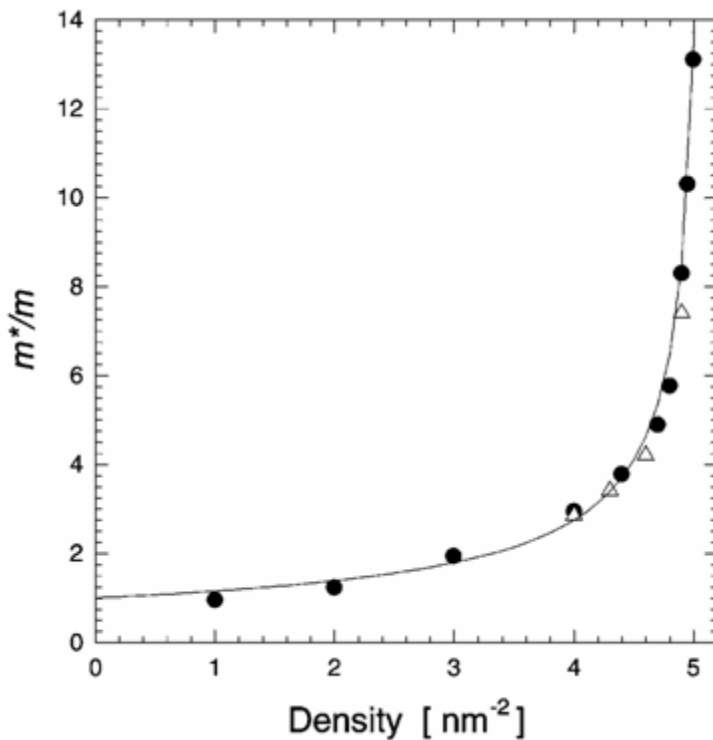
$$F(\mu) = \xi^{-d-z} f(\xi^{y_\mu} \mu)$$

$$y_\mu = 4, \quad z = 4$$

MI, JPSJ 64 (1995) 2954

^3He ; unusual degeneracy temperature

$$C = \gamma T + \Gamma_{2D} T^2$$



$$m^*/m \propto 1/\delta n$$

$$T_F \propto \delta n^2$$

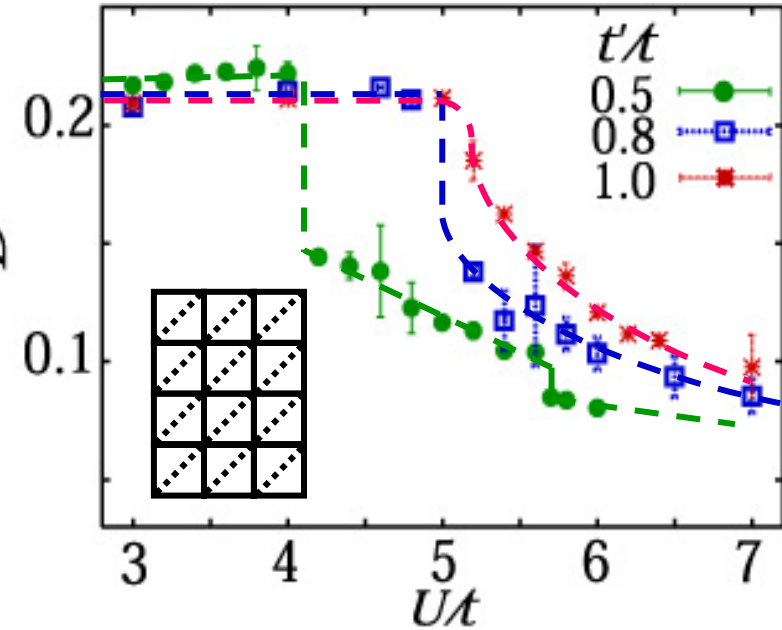
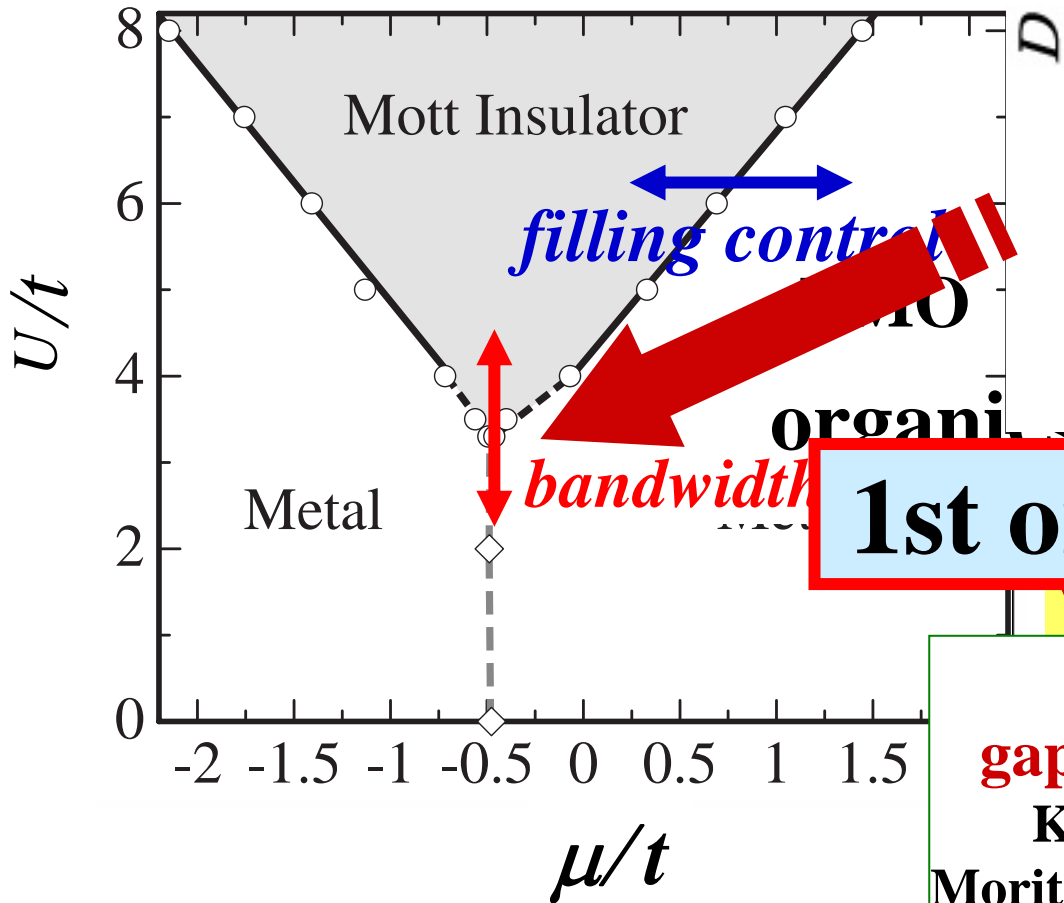
Casey et al. PRL 90 (2003) 115301

Phase Diagram of Mott Transition in the 2D Hubbard model

経路積分繰り込み群法

PIRG numerical results

$$t = 1, t' = -0.2$$



1st order transition

v shape boundary

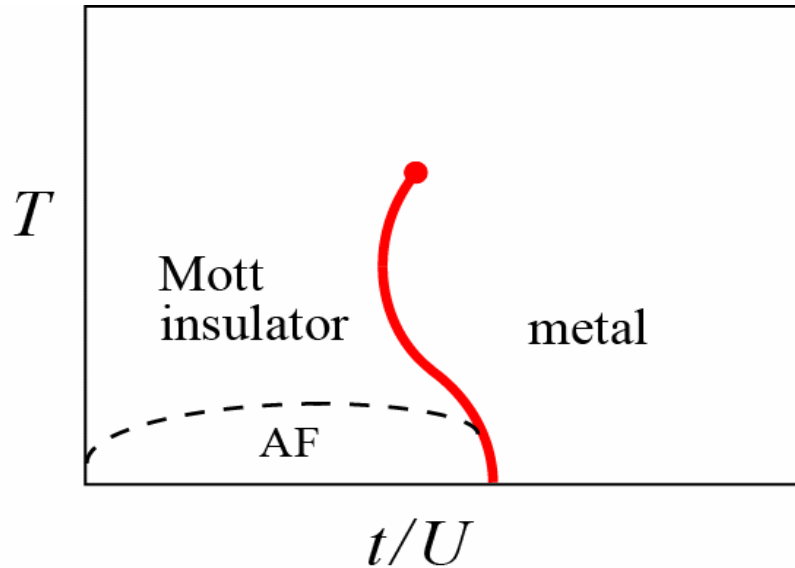
Lower T_c at larger t'

gapless quantum spin liquid

Kashima, Imada, JPSJ(2001)

Morita, Watanabe, Imada, JPSJ(2002)

Advantage of Bandwidth Control MIT

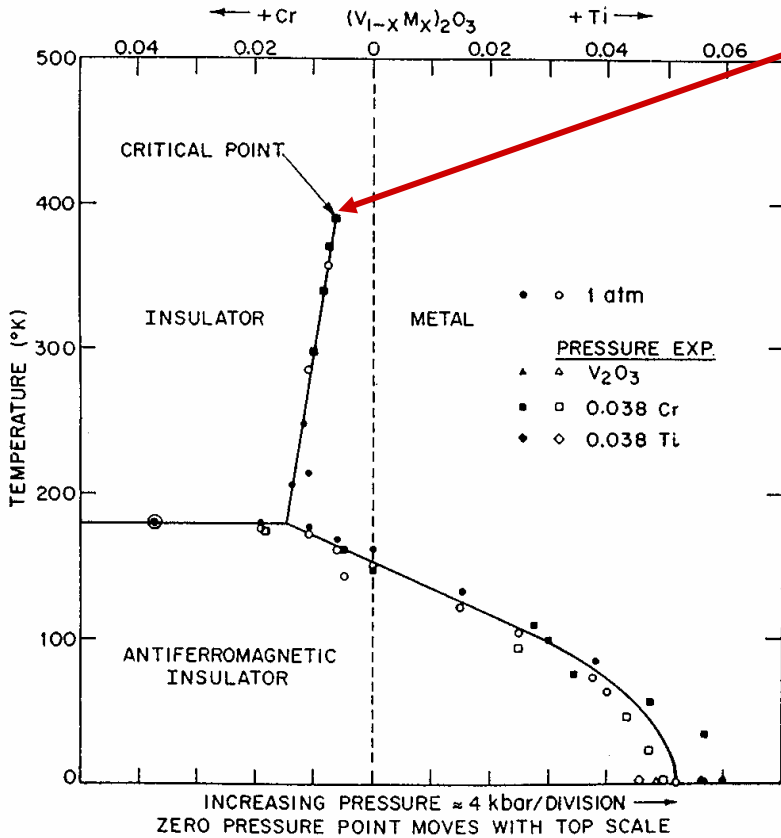


- ★ Small energy scale;
suppress Multi-furcation
- ★ Absence of other orders; AF...
- ★ Absence of long-range
Coulomb effect
 \Leftrightarrow ${}^3\text{He}$

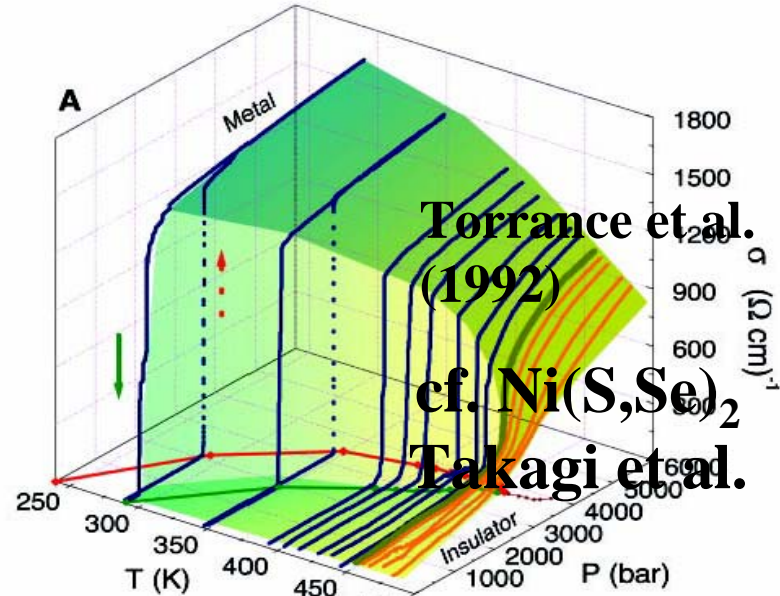
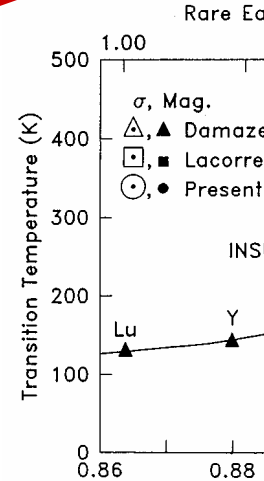
**“Pure” Mott transition
arising from short-ranged repulsion**

Bandwidth Control MIT

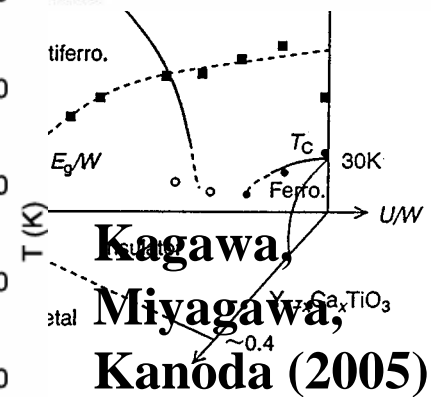
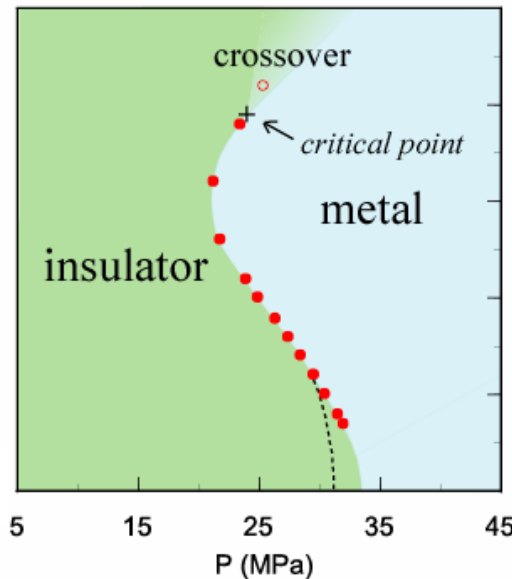
Ising criticality
Limelette et al. (2003)



V_2O_3 McWhan et al. (1972)



Torrance et al. (1992)
cf. $Ni(S,Se)_2$
Takagi et al.



$\kappa-(ET)_2Cu[N(CN)_2]Cl$

Breakdown of Ginzburg-Landau-Wilson scheme

Ginzburg-Landau-Wilson scheme に従わない相転移

$$F = -\mu X + aX^{(d+2)/d} + bX^{(d+4)/d} \quad T = 0$$

$a > 0$; continuous transition ($T_c = 0$)
quantum region

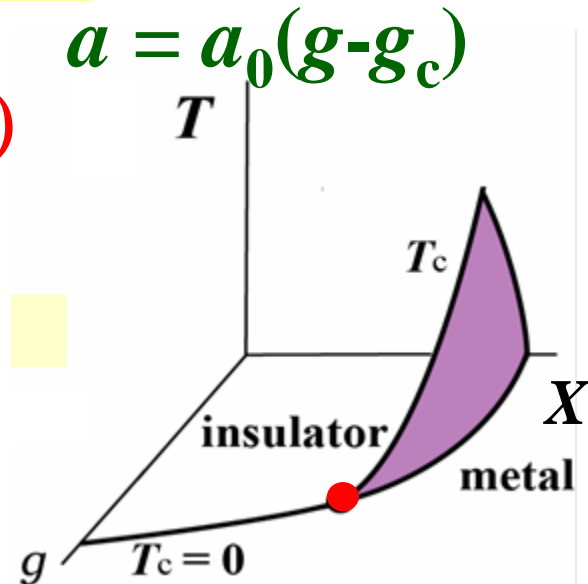
$\mu > 0$; metal: $\mu < 0$; insulator

$a < 0$; first order

$a \rightarrow 0$ Marginally quantum critical point (MQCP)

unusual QCP

M. IMADA



Unusual Critical Exponents at MQCP

$$\beta = d/2, \gamma = 2 - d/2, \delta = 4/d, \nu = 1/2,$$

$$z = 4$$

Ginzburg criterion

$$d + z_t \geq (2\beta + \gamma)/\nu = d + 4$$

All the dimensions are at the upper critical dimension

**“mean field” is basically correct,
while hyperscaling is satisfied**

2次元 $\beta = 1, \gamma = 1, \delta = 2, \nu = 1/2,$

$$z = 4$$



Kagawa, Miyagawa, Kanoda *M. IMADA*

Consequence of Diverging Density Fluctuations

filling control; electron density fluctuation
bandwidth control; excitonic fluctuation

$$\chi = (d^2 F / dX^2)^{-1} \sim (aX^{2/d-1} + bX^{4/d-1})^{-1}$$

Marginal quantum critical point; $a \rightarrow 0$

$$\chi \sim X^{1-4/d}$$

秩序化に伴うゆらぎとは別の
波数0近傍の独立なゆらぎ

$$\chi_c(q, \omega) = \frac{\Gamma^{-1}}{-i\omega + D_s(K^2 + (q - Q)^2)}$$

large energy scale; Mott gap

example; 2D

contrast with spin/orbital fluctuations; $J \Leftrightarrow$ Mott gap

Outlook for Super Clean Project

電子やヘリウムの密度自由度が引き起こす
1次転移の消える瀬戸際の物理の確立

Mott
charge order
valence
Lifshitz

1次転移の背景となる
高いエネルギースケール

Summary

Band-width control & filling-control
unified description of quantum Mott criticality
Beyond GLW scheme; unusual universality class

d dependent critical exponents

bandwidth control transitionでの検証

marginal quantum criticality (MQCP)

diverging density (charge) fluctuations

large energy scale \sim Mott gap, small q

incoherent response up to high energy

competing orders

(1) electron differentiation \Rightarrow ARPES structure

(2) tendency for inhomogeneity

(3) density fluctuations drive non-Fermi liquid properties

superconducting mechanism

d-wave, high- T_c

Outlook

accurate $\varepsilon(\mathbf{k}, \omega)$

Mott
charge order
valence
Lifshitz

filling control
bandwidth control